

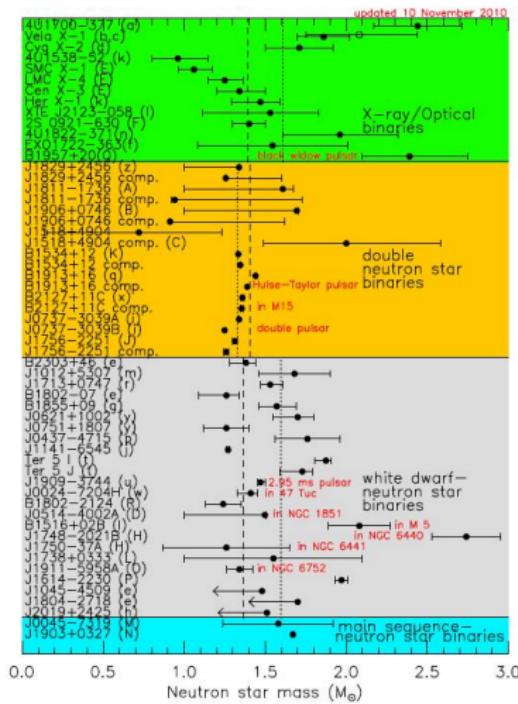
# Hyperon stars

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# Neutron star masses - results of measurements



Massive neutron stars:  
neutron star – white dwarf binary  
systems

P.Demorest et al. Nature (2010)

- PSR J1614-2230

- $M_{NS} = 1.97 \pm 0.04 M_{\odot}$
- $M_{WD} = 0.5 \pm 0.006 M_{\odot}$

Antoniadis et al. Science (2013)

- PSR J0348+0432

- $M_{NS} = 2.01 \pm 0.04 M_{\odot}$
- $M_{WD} = 0.172 \pm 0.003 M_{\odot}$

# Tolmann-Oppenheimer-Volkoff (TOV) equations of hydrostatic equilibrium

The equilibrium of a spherically symmetric star

$$\frac{dP}{dr} = \frac{-G(\rho(r) + P(r))(m(r) + 4\pi r^3 P(r))}{r^2 \left(1 - \frac{2Gm(r)}{r}\right)}$$

$$\frac{dm}{dr} = 4\pi r^2 \rho(r)$$

$P(r)$  and  $\rho(r)$  - pressure and density at radial coordinate  $r$

Solution of TOV equations requires the knowledge of the equation of state (EoS) of dense asymmetric nuclear matter  $\rightarrow P(\rho)$

- gives M-R relation
- enables modeling of the internal structure of a neutron star

**Solution of TOV equations provides data on the impact of a given model on the internal structure of a neutron star**

# Maximum mass of a neutron star

For calculated EoS there exists the maximum achievable neutron star mass  $M_{max}$ .

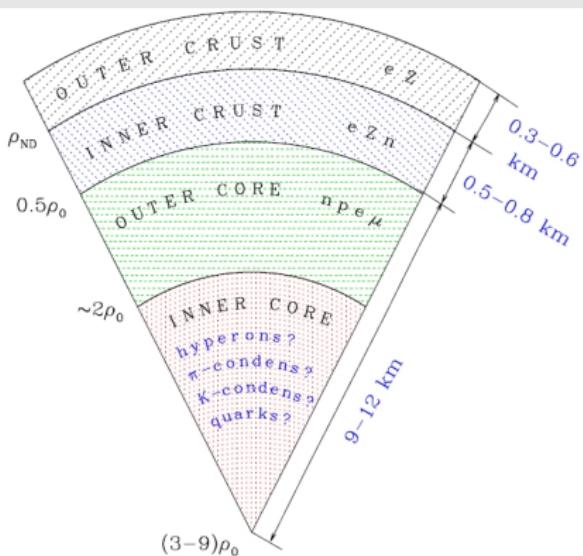
Maximum mass of a neutron star is a decisive factor for observational distinguishing between neutron stars and black holes.  
The following condition has to be satisfied:

**Measured neutron star masses  $\leq M_{max}$ :**

- limits the value of a neutron star mass
- constrains the EoS of high density nuclear matter
  - lower value of  $M_{max}$  - softer EoS - results obtained for binary neutron stars:  $M_{obs} \sim 1.4M_{\odot} \leq M_{max}$
  - higher value of  $M_{obs} \simeq M_{max}$  - stiff EoS, massive neutron stars: PSR J1614-2230 and PSR J0348+0432

# Neutron star structure

## Schematic structure of a neutron star



- atmosphere
- outer crust - lattice of neutron-rich heavy nuclei, degenerate, relativistic electrons - correction to radius
- inner crust - as above plus degenerate non-relativistic neutrons
- outer core - homogeneous nucleonic matter
- inner core - may contain exotic forms of matter

# Characteristics of the matter of a neutron star

- $\beta$ -stable nuclear matter
  - $p + e^- \leftrightarrow n + \nu_e$
  - $n \leftrightarrow p + e^- + \bar{\nu}_e$
- cold, neutrino-free matter  $\mu_{\nu_e} = \mu_{\bar{\nu}_e} = 0$
- $\sum_i Q_i n_i = 0$
- $n_B = \sum_i B_i n_i$
- $\mu_i = B_i \mu_i - Q_i \mu_e$
- Constituents of the model:
  - baryons:  $N \cup \{\Lambda, \Sigma^+, \Sigma^0, \Sigma^-, \Xi^0, \Xi^-\}$
  - leptons:  $L \in \{e^-, \mu^-\}$
  - mesons:  $M \in \{\sigma, \omega_\mu, \rho_\mu^a\} \cup \{\sigma^*, \varphi_\mu\}$  ← introduced to describe YY interaction

# The model

- Lagrangian of the model:  $\mathcal{L} = \mathcal{L}_0 + \mathcal{L}_{nonl}^M$
- $\mathcal{L}_0$  includes contributions from baryons and mesons
- $\mathcal{L}_{nonl}^M$  the part describing meson interactions

$$\mathcal{L}_{nonl}^M = U_{scalar}(\sigma) + U_{vec}(\omega, \rho, \varphi)$$

$$U_{scalar}(\sigma) = 1/3g_3\sigma^3 + 1/4g_4\sigma^4$$

$$U_{vec}(\omega, \rho, \phi) = U_{vec}^{S=0}(\omega, \rho) + U_{vec}^S(\omega, \rho, \phi)$$

When the matter of the neutron star includes only nucleons the vector meson potential reduces to the part

$$\begin{aligned} U_{vec}^{S=0}(\omega, \rho) &= \frac{1}{4}c_3(\omega^\mu \omega_\mu)^2 + \frac{1}{4}c_3(\rho^{\mu a} \rho_\mu^a)^2 + \\ &+ \Lambda_V(g_N \omega g_N \rho)^2 (\omega^\mu \omega_\mu)(\rho^{\mu a} \rho_\mu^a). \end{aligned}$$

# The case of non-strange matter

## Extended isovector sector

$$E_{sym}(n_B) = \frac{k_F^2}{\sqrt{(k_F^2 + M_{eff}^2)}} + \frac{\rho}{8(m_\rho^2/g_{N\rho}^2 + 2\Lambda_V(g_{N\omega}\omega)^2)}$$

- $\omega - \rho$  meson coupling → modification of the high density limit of the symmetry energy
- the parameter  $g_{N\rho}$  is adjusted to reproduce the symmetry energy  $E_{sym} = 25.68$  MeV at  $k_F = 1.15\text{fm}^{-1}$
- the density slope of the symmetry energy L - current experimental results: 40.5 – 61.9 MeV

# Coupling constants

Baryon–vector meson coupling constants are estimated on the basis of SU(6) symmetry.

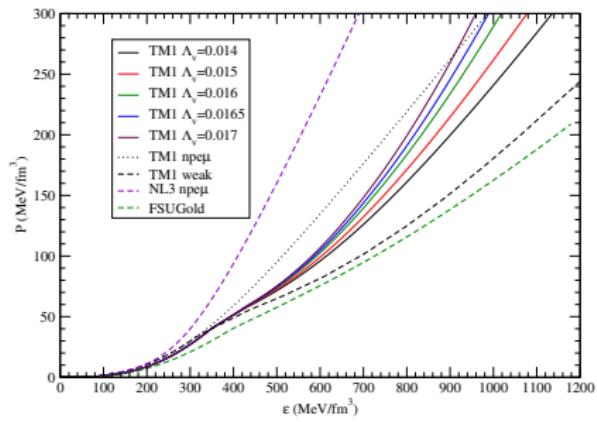
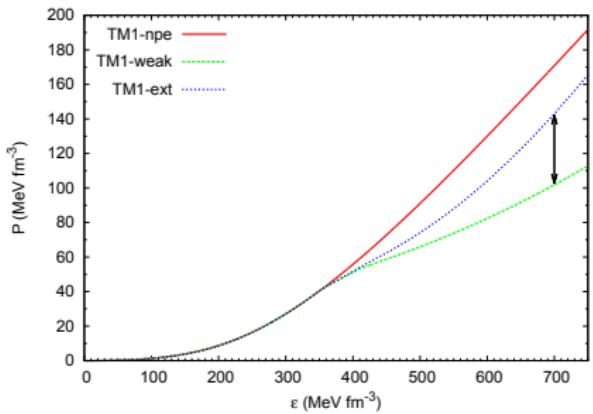
Scalar and vector coupling constants are strongly correlated - fixed by the potential depth of the corresponding hyperons:

$$U_{\Lambda}^{(N)} = -28 \text{ MeV}, \quad U_{\Sigma}^{(N)} + 30 \text{ MeV}, \quad U_{\Xi}^{(N)} = -18 \text{ MeV}.$$

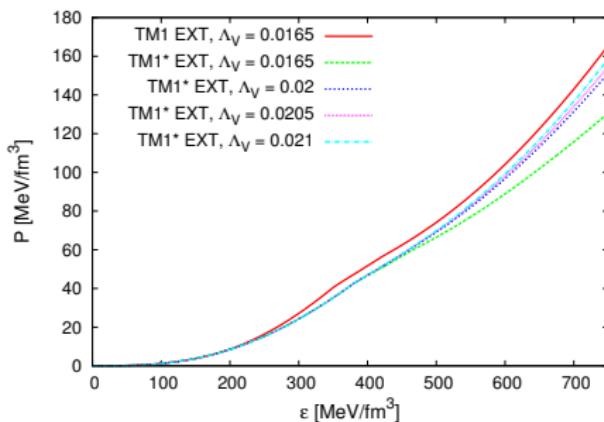
The coupling constants of hyperons to the meson  $\sigma^*$  were calculated from relations:

$$U_{\Xi}^{(\Xi)} \simeq U_{\Lambda}^{(\Xi)} \simeq 2U_{\Xi}^{(\Lambda)} \simeq 2U_{\Lambda}^{(\Lambda)}.$$

# Equation of State



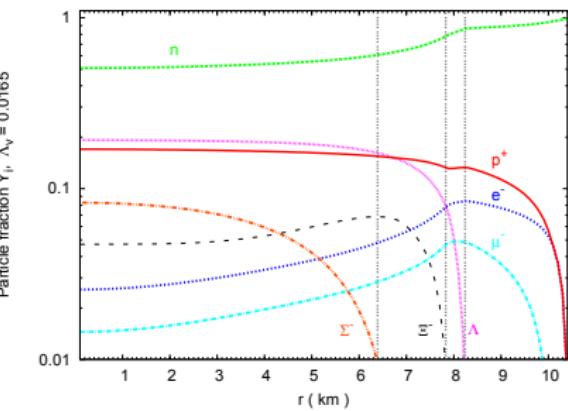
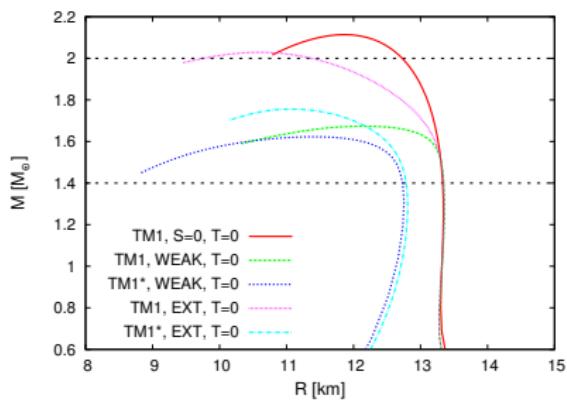
# Equation of State



## TM1\* parameter set

- modification of TM1 parameter set
- inclusion of scalar-vector meson coupling constant
- improvement of density slope of symmetry energy

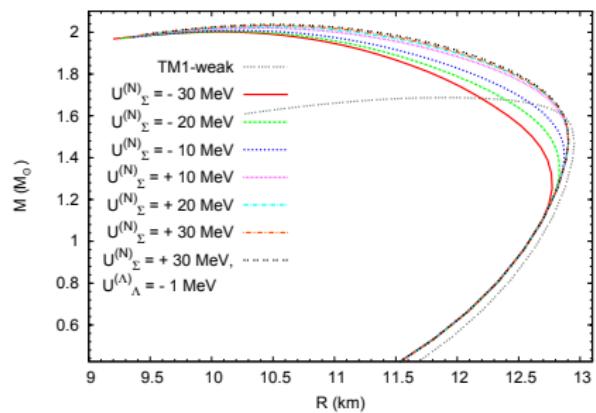
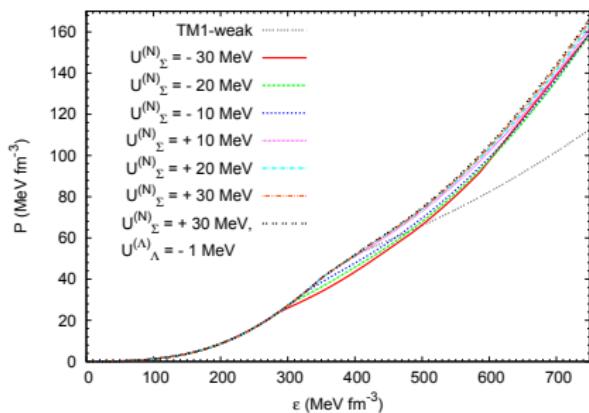
# M-R relations and the structure of a neutron star



# The effect of the $U_Y^{(N)}$ potential

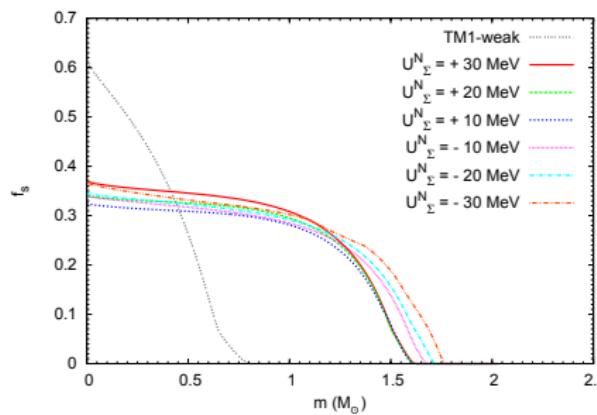
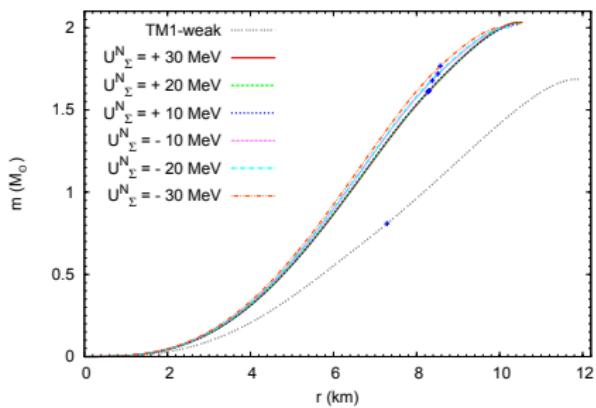
## Implications for neutron stars

- bulk properties of a neutron star
- structure and composition of a neutron star

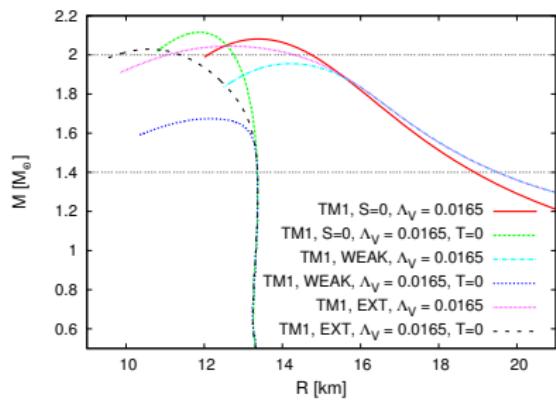
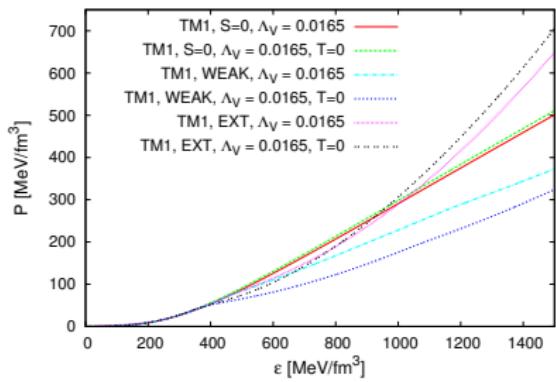


Results obtained for different values of the  $U_A^{(N)}$  potential.

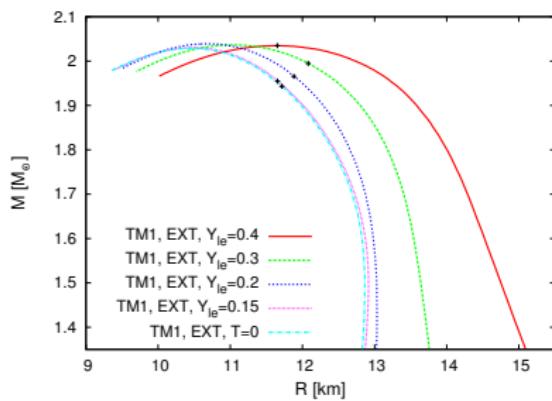
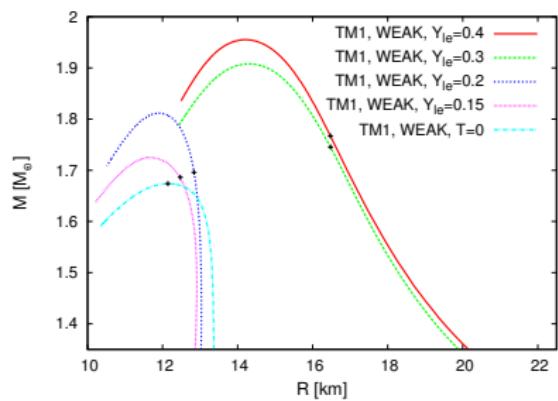
# Internal structure of the maximum mass configurations



# Neutron star evolution



# Neutron star evolution



## Conclusions

- Neutron stars with hyperons - reduction of masses
- Solution - extra repulse is needed
- Alternative solution - strange quark matter

Thank you for your attention!